

S.No. : 391

BEC 2601

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Following Paper ID and Roll No. to be filled in your Answer Book.

PAPER ID : 23456

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B. Tech. Examination 2021-22

(Even Semester)

DIGITAL SIGNAL PROCESSING

Time : Three Hours]

[Maximum Marks : 60

Note :- Attempt all questions.

SECTION – A

1. Attempt all parts of the following : $8 \times 1 = 8$
 - (a) Write down the expression for one sided z transform.
 - (b) Explain linearly property of Z transform.
 - (c) What do you meanby periodictiy of the DFT?
 - (d) Define causal systems.

[P. T. O.

- (e) What is the minimum sampling rate required to avoid aliasing for the signal

$$x(t) = 2 \cos 100 \pi t$$

- (f) Write down the condition for a real valued sequence $X(n)$ to be an even sequence.
- (g) Determine if the systems described by :

$$y(n) = n x(n)$$

is linear or non-linear.

- (h) Write down the statement of initial value theorem.

SECTION – B

2. Attempt any two parts of the following : $2 \times 6 = 12$

- (a) Determine the z transform of the following finite duration signals :

$$(i) \quad x(n) = \left\{ \begin{array}{ccccccc} 3 & 1 & 2 & 5 & 7 & 0 & 1 \\ & & & \uparrow & & & \end{array} \right\}$$

$$(ii) \quad x(n) = \left\{ \begin{array}{ccccccc} 2 & 4 & 5 & 7 & 0 & 1 & 2 \\ & & \uparrow & & & & \end{array} \right\}$$

$$(iii) \quad x(n) = \{0, 0, 1, 2, 5, 4, 0, 1\}$$

- (b) Explain in detail the chirp-z algorithm.
- (c) Determine the unit sample response of the ideal low pass filter. Also prove that it is not realizable.
- (d) Show that the convolution in time domain is the same as product in frequency domain.

SECTION – C

Note :- Attempt all questions. Attempt any two parts from each questions. 5×8=40

3. (a) Determine the inverse z transform of :

$$X(z) = \frac{z}{3z^2 - 4z + 1}$$

if the ROC are :

(i) $|z| > 1$

(ii) $|z| < \frac{1}{3}$

- (b) Determine the DFT of the following sequence :

$$x(n) = \begin{cases} \frac{1}{4}, & \text{for } 0 \leq n \leq 2 \\ 0, & \text{otherwise} \end{cases}$$

[P. T. O.]

- (c) Perform the circular convolution of the following two sequences :

$$x_1(n) = \left\{ \begin{array}{cccc} 2 & 1 & 2 & 1 \\ \uparrow & & & \end{array} \right\}$$

$$x_2(n) = \left\{ \begin{array}{cccc} 1 & 2 & 3 & 4 \\ \uparrow & & & \end{array} \right\}$$

4. (a) Determine DFT (8-point) for a continuous time signal $x(t) = \sin(2\pi ft)$ with $f = 50$ Hz.
- (b) Establish the relationship between DFT and z transform.
- (c) Obtain direct form I and II realizations for a third order HR transfer function :

$$H(z) = \frac{0.28z^2 + 0.319z + 0.04}{0.5z^3 + 0.3z^2 + 0.17z - 0.2}$$

5. (a) Explain Goertzel algorithm for efficient DFT computation.
- (b) Develop cascade and parallel realization structures for the following :

$$H(z) = \frac{\frac{z}{6} + \frac{5}{24} + \left(\frac{5}{24}\right)z^{-1} + \frac{1}{24}z^{-2}}{1 - \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2}}$$

- (c) A low pass filter has the desired response as given below :

$$H_d(e^{j\omega}) = \begin{cases} e^{-j\omega} & , 0 \leq \omega < \frac{\pi}{2} \\ 0 & , \frac{\pi}{2} \leq \omega \leq \pi \end{cases}$$

Determine the filter coefficients $h(n)$ for $M = 7$, using Type-I frequency sampling technique.

6. (a) An analog filter has the following system function. Convert this filter into a digital filter using backward difference for the derivative :

$$H(s) = \frac{1}{(s + 0.1)^2 + 9}$$

- (b) Explain the design of IIR filter by the bilinear transformation method. What are the advantages and disadvantages of this method?
- (c) Explain the design of Hilbert transform. What are the applications of Hilbert transform?
